Transcript of "Symbolic Logic Rap" by Ewan Kingston

video and slides: https://ewan-kingston.net/symbolic-logic-rap/

- Rules are those used in Power of Logic by Howard-Snyder, Howard-Snyder and Wasserman (McGraw Hill)
- Not included Quantifier Negation, Identity.
- You might learn a slightly different collection of rules in your class or textbook, or use different names for the same rules.

[8 Implicational rules]

8 implicational rules, use them only on whole lines they're powerful tools.

When two things are your options and suddenly one isn't/ That's DS – <u>Disjunctive Syllogism</u>.
If p then q....p Whaddya get?/ q: <u>Modus ponens</u>, its famous, don't forget.
If p then q, but want not p then?/ If you have not q you can, that's <u>Modus Tollens</u>.
Now two conditionals make a single chain/ From the first to the last, <u>Hypothetical syllogism</u>'s the name.
<u>Constructive dilemma</u>'s a 4 line move/ p or q to r or s via conditionals, 2
<u>Conjunction</u>'s in the name, you get to use one/ If you have both sides of the conjunction.
<u>Simplification</u> is the reverse indeed/ p and q splits to p (or q) alone as you need.
Addition is a weird thing/ p gives you p or anything

8 implication rules, don't run em in reverse. You want rules like that? They're in the next verse.

[10 Equivalence rules]

Equivalence rules work both ways. The first statement says what the second one says.

If you want two tildes, use <u>Double Negation</u>/ It also works for two-tilde elimination <u>Commutation</u> is <u>easy</u>/ Just see p or q as q or p [same with and] <u>Association</u> shuffles the parentheses/ It only works with all dots and all vees <u>DeMorgan's laws</u>: for "not both" and neither-nor/ Drop/add parentheses, swap ands and ors With the material conditional, you can do a lot/ <u>Contraposition</u> switches the order and adds <u>two nots</u>. If you have p v p, you can have p for free/ p gives "p and p" that's <u>Redundancy</u> Got a conjunction for an antecedent? /<u>Export</u> one side to be a prior antecedent. Sharing's caring – <u>Distribution</u> can give you more/ One P is distributed across an and or an or. <u>Material implication</u> – an arrow to a v/ You just gotta negate the antecedent, see? Biconditionals are changed by <u>Material Equivalence/</u> p if q and only if q, you see its relevance It's also equivalent to either-both-or-neither/ Check the truth table if you're not a believer

You can use equivalence rules on parts of lines/ Good for when that proof is giving you hard times.

[4 rules of predicate logic]

To deal with quantifiers, four new rules/ Two of them fussy, two of them cool

All means everything single thing/ So <u>instantiate</u> a <u>universal</u> with no restrictions If it happens to this, it happens to something, agree?/<u>Existential Generalization</u>: EG <u>Existential Instantiation</u> brings a cameo/ Constant comes from nowhere then away it goes <u>UG</u> lets you generalize from anything/ If you only know about the instance what you know about everything

22 rules for natural deduction proofs/ They can show validity because they preserve truth